

Please write clearly in block capitals.

Centre number

--	--	--	--	--

Candidate number

--	--	--	--

Surname

Forename(s)

Candidate signature

I declare this is my own work.

A-level FURTHER MATHEMATICS

Paper 2

Time allowed: 2 hours

Materials

- You must have the AQA Formulae and statistical tables booklet for A-level Mathematics and A-level Further Mathematics.
- You should have a scientific calculator that meets the requirements of the specification.

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer each question in the space provided for that question. If you require extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do **not** write outside the box around each page or on blank pages.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 100.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.

For Examiner's Use	
Question	Mark
1	
2	
3	
4	
5	
6	
7	
8	
9	
10	
11	
12	
13	
14	
TOTAL	



Answer **all** questions in the spaces provided.

- 1** Find the imaginary part of

$$\frac{5+i}{1-i}$$

Circle your answer.

[1 mark]

−3

−2

2

3

- 2** Find the mean value of the function $f(x) = 10x^4$ between $x = 0$ and $x = a$

Circle your answer.

[1 mark]

$10a^3$

$40a^3$

$2a^4$

$4a^5$



3 The roots of the equation $x^2 - px - 6 = 0$ are α and β

Find $\alpha^2 + \beta^2$ in terms of p

Circle your answer.

[1 mark]

$$p^2 - 6$$

$$p^2 + 6$$

$$p^2 - 12$$

$$p^2 + 12$$

4 Which of the following graphs intersects the graph of $y = \sinh x$ at exactly one point?

Circle your answer.

[1 mark]

$$y = \operatorname{cosech} x$$

$$y = \cosh x$$

$$y = \coth x$$

$$y = \operatorname{sech} x$$

Turn over for the next question

Turn over ►

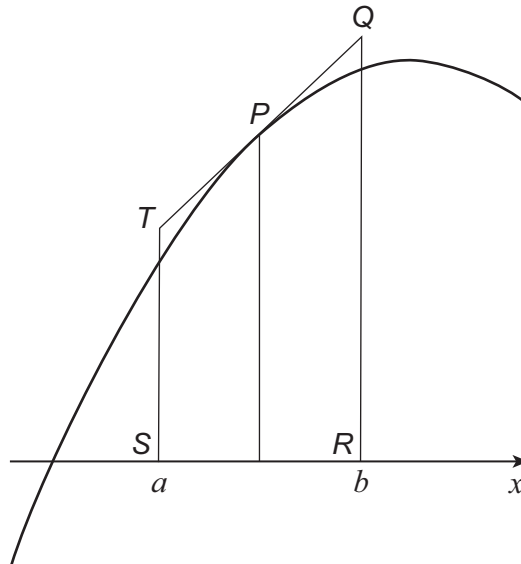


6 The diagram below shows part of the graph of $y = f(x)$

The line TPQ is a tangent to the graph of $y = f(x)$ at the point $P\left(\frac{a+b}{2}, f\left(\frac{a+b}{2}\right)\right)$

The points $S(a, 0)$ and T lie on the line $x = a$

The points Q and $R(b, 0)$ lie on the line $x = b$



Sharon uses the mid-ordinate rule with one strip to estimate the value of the integral $\int_a^b f(x) dx$

By considering the area of the trapezium $QRST$, state, giving reasons, whether you would expect Sharon's estimate to be an under-estimate or an over-estimate.

[3 marks]

Turn over ►



9 (b) (ii) Given that y satisfies the differential equation in part **(b)(i)** and that $y = 12.3$ when $x = 5$, find the value of y when $x = 5.2$

Give your answer to six significant figures.

[3 marks]

9 (c) Comment on the accuracy of your answer to part **(a)**.

[1 mark]

Turn over ►



11 (b) (i) Describe how the directions of the invariant lines of the transformation represented by **M** are related to each other.

Fully justify your answer.

[2 marks]

11 (b) (ii) Describe fully the transformation represented by **M**

[2 marks]

Turn over for the next question

Turn over ►

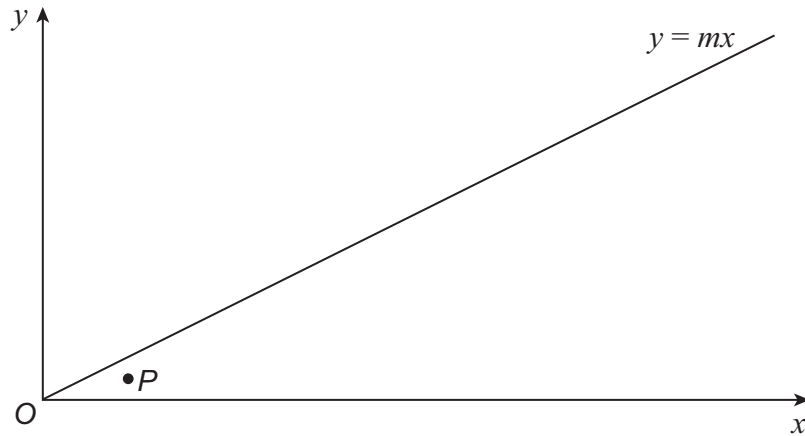


13 (c) (i) The diagram below shows a point P and the line $y = mx$

Draw four lines on the diagram to demonstrate the result proved in part (b).

Label as P' the image of P under the transformation represented by $(BA)^2$

[2 marks]



13 (c) (ii) Explain how your completed diagram shows the result proved in part (b).

[2 marks]



14

On an isolated island some rabbits have been accidentally introduced.

In order to eliminate them, conservationists have introduced some birds of prey.

At time t years ($t \geq 0$) there are x rabbits and y birds of prey.

At time $t = 0$ there are 1755 rabbits and 30 birds of prey.

When $t > 0$ it is assumed that:

- the rabbits will reproduce at a rate of $a\%$ per year
- each bird of prey will kill, on average, b rabbits per year
- the death rate of the birds of prey is c birds per year
- the number of birds of prey will increase at a rate of $d\%$ of the rabbit population per year.

This system is represented by the coupled differential equations:

$$\frac{dx}{dt} = 0.4x - 13y \quad (1)$$

$$\frac{dy}{dt} = 0.01x - 1.95 \quad (2)$$

14 (a)

State the value of a , the value of b , the value of c and the value of d

[2 marks]

14 (b)

Solve the coupled differential equations to find both x and y in terms of t

[9 marks]



There are no questions printed on this page

*Do not write
outside the
box*

**DO NOT WRITE ON THIS PAGE
ANSWER IN THE SPACES PROVIDED**



