

Lesson 2 – Commutativity and Strategies for Addition/Subtraction

Starter

- 1) $234 + 129$
- 2) $0.35 + 2.367$
- 3) $673 - 388$
- 4) $34.57 - 1.236$
- 5) $0.129 + 11.2362$

Starter Answers

- 1) 363 2) 2.717 3) 285 4) 33.334 5) 11.3652

Operations are **commutative** if they can be carried out in any order and still get the same answer.

For example, **addition** is commutative since we could do $2 + 3$ or $3 + 2$ and still get 5 as the answer.

Example 1

Decide whether these operations are commutative or not. Write down an example to demonstrate each one.

- 1) Multiplication
- 2) Subtraction
- 3) Division

Answers

1) Multiplication is **commutative**. For example, we could do 4×5 or 5×4 and still get 20 as the answer.

We could do this with any number of values. For example, if we had $2 \times 3 \times 4$ this would be the same as $3 \times 2 \times 4$ or $4 \times 2 \times 3$ etc.

2) Subtraction is **not commutative**. For example, $3 - 5 \neq 5 - 3$ (\neq means not equal to)

3) Division is **not commutative**. For example, $10 \div 5 \neq 5 \div 10$

For **additions** and **subtractions**, we are allowed to change the order of the calculation as long as we are performing the correct operations to the correct numbers.

Example 2

Place one of these signs (= or \neq) between these sets of calculations

1) $14 + 5 - 9$ $14 - 9 + 5$

In both calculations, we are doing two operations to 14. We are doing +5 and -9. It does not matter which order we do this in, as long as the 5 is being added and the 9 is being subtracted.

So, we have $14 + 5 - 9 = 14 - 9 + 5$

2) $23 - 10 + 3$ $23 + 10 - 3$

We are doing two operations to 23.

We are subtracting 10 in the first one but adding 10 in the second one.

Similarly, we are adding 3 in the first one but subtracting 3 in the second.

So, these calculations are not equal.

$23 - 10 + 3 \neq 23 + 10 - 3$

3) $18 - 6 + 2$ $6 - 18 + 2$

$18 - 6$ is not equal to $6 - 18$ since subtraction is not commutative.

We are then adding 2 to both calculations.

So therefore $18 - 6 + 2 \neq 6 - 18 + 2$

Your go

Place one of these signs (= or \neq) between each calculation

1) $16 + 19 + 15$ $15 + 16 + 19$

2) $30 \div 2$ $2 \div 30$

3) $12 - 5 - 7$ $12 - 7 - 5$

4) $2 \times 4 \times 5 \times 6$ $4 \times 6 \times 5 \times 2$

5) $15 + 8 - 9$ $15 - 8 + 9$

6) $26 - 7 + 12 - 2$ $26 + 12 - 7 - 2$

Answers

1) = 2) \neq 3) = 4) = 5) \neq 6) =

We can use these properties to make calculations easier to work out.

Example 3

Change the order to make the calculation easier: $23 + 15 + 7 + 5 + 2$

Look for pairs of numbers that add up to a multiple of 10

We know that $23 + 7 = 30$ and $15 + 5 = 20$ and $30 + 20$ is easy to work out.

So, since addition is commutative, we can change the calculation to:

$$23 + 7 + 15 + 5 + 2$$

$$= 30 + 20 + 2$$

$$= 52$$

Example 4

Change the order to make the calculation easier: $133 - 48 + 17 - 102$

Look for numbers that would add or subtract to make multiples of 10 or easier numbers.

We know $3 + 7 = 10$ so we could change the order to:

$$133 + 17 - 48 - 102$$

$$= 150 - 48 - 102$$

Subtracting 48 and then subtracting 102 means we have subtracted 150 in total ($48 + 102 = 150$).

$$= 150 - 150$$

$$= 0$$

Example 5

Change the order to make the calculation easier: $42 + 56 - 42$

We can change the order as long as we are adding 56 and subtracting 42

$$= 42 - 42 + 56$$

$$= 0 + 56$$

$$= 56$$

Your go

Change the order to make the calculation easier

1) $128 + 17 + 12 + 13$

2) $55 + 28 + 2 + 15 + 7$

3) $146 - 28 + 14 - 12 - 3$

4) $98 + 64 - 98 + 6$

Answers

1) 170

2) 107

3) 117

4) 70