

## UNIT 11 *Angles, Bearings and Maps*

## Activities

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### Activities

11.1 Independent Angles

11.2 Flight Paths

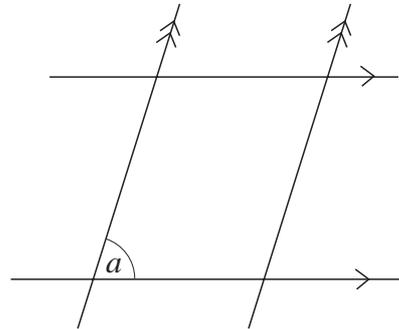
11.2a Flight Paths - Map

Notes and Solutions (1 page)

# ACTIVITY 11.1

## Independent Angles

In the diagram opposite, which has two pairs of parallel lines, giving just one angle, say  $a$ , means that all other angles are specified.

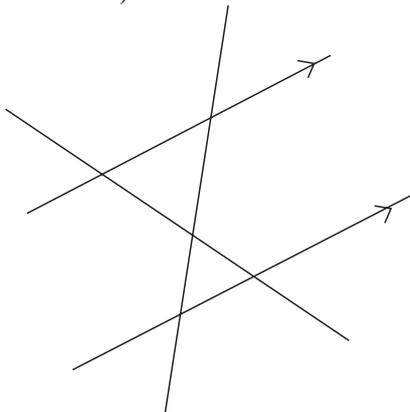


- Copy the diagram. Given that  $a = 65^\circ$ , mark the size of each of the other angles on your diagram.

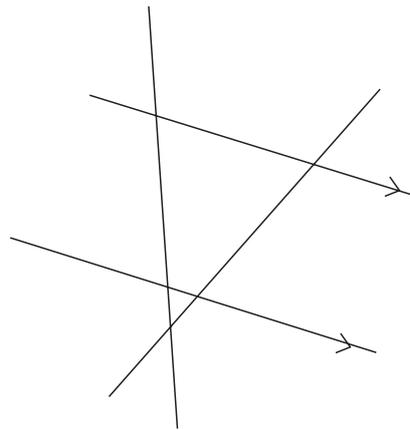
The number of 'independent' angles depends on the configuration, i.e. the number of lines drawn, and which lines are parallel; this is illustrated in the following problem.

- In each of the following diagrams, decide how many independent angles there are. (If it is not clear, see how many values you need to give before all the other angles can be found.)

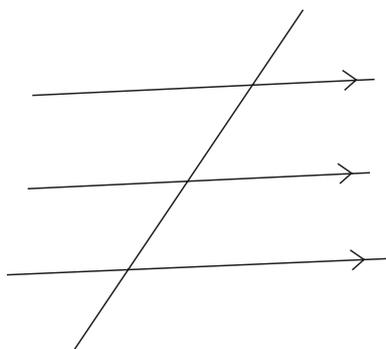
(a)



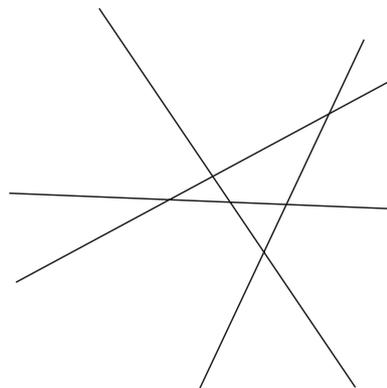
(b)



(c)



(d)



### Extension

Find the general formula for the number of independent angles when there are  $n$  lines, of which  $m$  pairs are parallel.

## ACTIVITY 11.2

## *Flight Paths*

The map of Britain given on Sheet Activity 11.2a is drawn to a scale of 1 : 3 000 000. Use the map to answer the following questions:

1. What are the bearings of:
  - (a) Newcastle,      (b) Edinburgh,      (c) Glasgow,      (d) Manchester
 from London? Also find the bearings *from* each of these cities *to* London.
  
2. (i) A plane leaves London at 1400 hours, travelling on a bearing of  $322^\circ$  at 480 km per hour.
  - (a) On Sheet Activity 11.2a, draw the flight path of the plane.
  - (b) How many kilometres will the plane travel in 30 minutes?
  - (c) On the map, which city might it have reached in that time?
  
- (ii) Another plane leaves Bristol at 1400 hours, travelling in the direction of Newcastle at a steady speed of 390 km per hour.
  - (a) Draw its flight path.
  - (b) Where will it be at 1425 hours?
  - (c) Design a new flight path which avoids the Manchester area by flying at least 30 km to the west, and then changing direction towards Newcastle. With the plane travelling at 390 km per hour, give the new flight path in the form

	<i>Bearing</i>	<i>Duration of Flight</i>
1		
2		

### *Extension*

You are the flight director of a new small airline based at Manchester. You have leased 4 identical planes which fly at an average speed of 450 km/h, and need refuelling after a maximum distance of 600 km. You would like to provide at least one daily return flight from Manchester to each of the other cities marked on the map.

Design: (a) *timetables* for the daily use of each plane (starting no earlier than 0700 hours, and finishing no later than 2200 hours; allow at least 40 minutes between arrival and departure at any airport).

(b) *flight paths* for all flight movements, ensuring that they do not conflict with one another.

# ACTIVITY 11.2a

## Flight Paths - Map

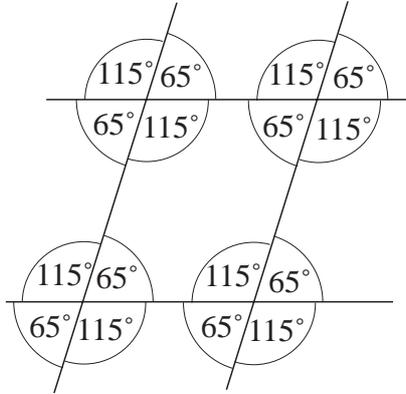
Map of UK drawn to scale 1 : 3 000 000



# ACTIVITIES 11.1 - 11.2

## Notes for Solutions

11.1 1.



Note that, although 2 angles ( $65^\circ$  and  $115^\circ$ ) are needed, they are not independent as  $65^\circ + 115^\circ = 180^\circ$ .

2. (a) 2                      (b) 2                      (c) 1                      (d) 3

*Extension*

Formula:  $n - m - 1$

- 11.2 1. (a)  $348^\circ$               (b)  $344^\circ$               (c)  $333^\circ$               (d)  $320^\circ$   
 $168^\circ$ ;  $164^\circ$ ;  $153^\circ$ ;  $140^\circ$

2. (i) (b) 240 km              (c) Manchester  
 (ii) (b) Very close to the London - Manchester flight (maybe at a different height!).  
 (c) Possible answer:

	<i>Bearing</i>	<i>Duration of Flight</i>
1	$357^\circ$	30 mins
2	$032^\circ$	30 mins

*Extension* Various alternatives